

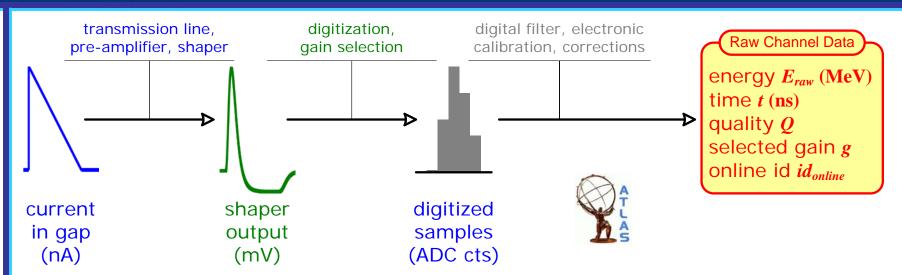
Peter Loch University of Arizona

Tucson, Arizona-USA



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Calorimeter Response



What is response?

Reconstructed calorimeter signal

Based on the direct measurement – the raw signal

May include noise suppression

Has the concept of signal (or energy) scale

Mostly understood as the basic signal before final calibrations

Does not explicitly include particle or jet hypothesis

Uses only calorimeter signal amplitudes, spatial distributions, etc.

$$E_{raw} = A_{peak} \times \underbrace{\left[\text{ADC} \rightarrow \text{nA}\right]}_{\text{visc}}$$

current calibration

 $\times \underbrace{([HV] \times [cross-talk] \times [purity])}$

electronic and efficiency corrections

 \times nA \rightarrow MeV

energy calibration



Slow signal collection in liquid argon calorimeters

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~450 ns @ 1 kV/mm drift time versus 40 MHz/25 ns bunch crossing time Measure only I₀ = I(t₀) (integrate <25 ns) Applying a fast bi-polar signal shaping

> Shaping time ~15 ns With well known shape

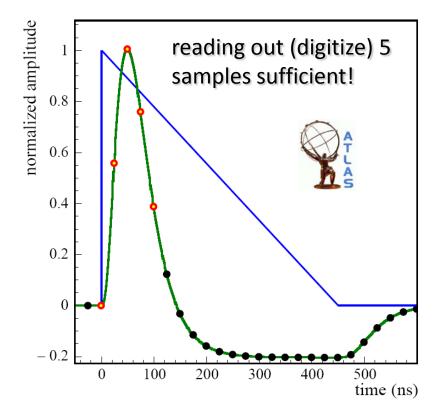
Shaped pulse integral = 0

Net average signal contribution from pile-up = 0

Need to **measure the pulse shape** (time sampled readout)

Total integration ~25 bunch crossings

23 before signal, 1 signal, 1 after signal





What is digital filtering

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Unfolds the expected (theoretical) pulse shape from a measured pulse shape

Determines signal amplitude and timing

Minimizes noise contributions

Noise reduced by ~1.4 compared to single reading

Note: noise depends on the luminosity

Requires explicit knowledge of pulse shape

> Folds triangular pulse with transmission line characteristics and active electronic signal shaping

Characterized by signal transfer functions depending on R, L, C of readout electronics, transmission lines

Filter coefficients from calibration system

Pulse "ramps" for response

Inject known currents into electronic chain

Use output signal to constrain coefficients

Noise for auto-correlation

Signal history couples fluctuations in time sampled readings

$$A_{\text{peak}} = \sum_{i=1}^{N_s} a_i (s_i - p)$$
 , with

digital filter coefficient \boldsymbol{a}_i reading in time sample pedestal reading

Signal peak time *t*_{neak}:

$$A_{\text{peak}}t_{\text{peak}} = \sum_{i=1}^{N_s} b_i (s_i - p)$$

W.E. Cleland and E.G. Stern, Nucl. Inst. Meth. A338 (1994) 467.

S_i

р





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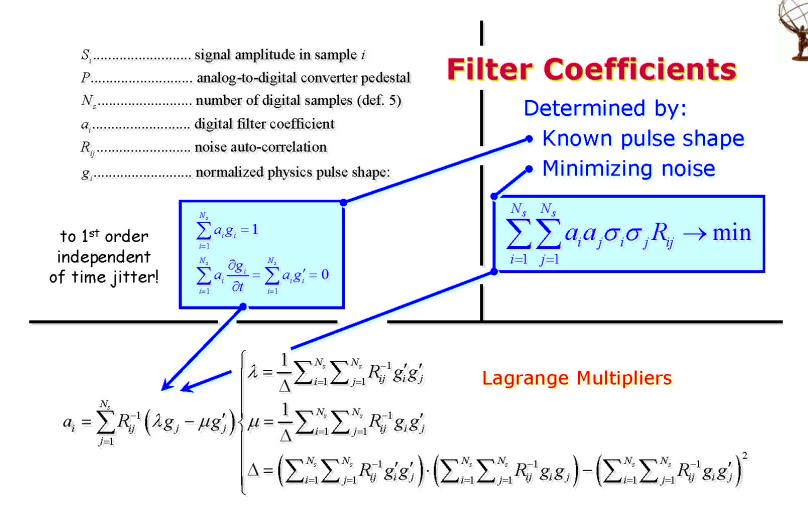
Constraints for digital filter coefficients *a*_i:

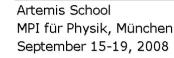
 $\sum a_i g_i = 1$, with g_i being the

normalized physics pulse shape

$$\sum_{i=1}^{N_{\rm s}} a_i \frac{\partial g_i}{\partial t} = 0$$







Slide *15* Peter Loch September 17, 2008



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What does signal or energy scale mean?

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Indicates a certain level of signal reconstruction

Standard reconstruction often stops with a basic signal scale

Electromagnetic energy scale is a good reference

> Uses direct signal proportionality to electron/photon energy

Accessible in test beam experiments

Can be validated with isolated particles in collision environment

Provides good platform for data and simulation comparisons

Does not necessarily convert the electron signal to the true photon/electron energy!

Hadronic signals can also be calculated on this scale

Good platform for comparisons to simulations

But does not return a good estimate for the deposited energy in noncompensating calorimeters – see later discussion!

Is not a fundamental concept of physics!

Is a calorimeter feature Definition varies from experiment to experiment

Recall electrons/photons in sampling calorimeters:

$$\mathbf{E}_{\rm vis} = \mathbf{N}_{\rm x} \int_{0}^{d_{\rm active}} \frac{dE}{dx} dx = \mathbf{N}_{\rm x} \Delta E \propto \mathbf{E}_{0}$$

Electron sampling fraction S_a relates signal and deposited energy:

$$S_{e} = \frac{E_{vis}}{E_{dep}} \approx \frac{E_{vis}}{E_{0}} \rightarrow \frac{E_{rec}^{em}}{S_{e}} = \frac{1}{S_{e}} E_{vis} = \frac{C_{e}A}{E_{dep}} \approx \frac{E_{o}}{E_{o}}$$

with *c* being the electron calibration constant.

(*S*[°] is a unitless fraction, *c*[°] converts a signal unit into an energy unit, e.g. $nA \rightarrow MeV$)

Response often denoted $e = e(E_{dep}) = E_{rec}^{em}(c_e, A)$



Hadronic Response (1)

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Single hadron reponse:

$$\pi(E_0) = f_{em}(E_0) \cdot e + (1 - f_{em}(E_0)) \cdot h$$

with
$$\begin{cases} f_{em}(E_0) & \text{intrinsic em fraction} \\ & \text{response of pure} \\ h & \text{hadronic shower branch} \end{cases}$$

Non-compensation measure:

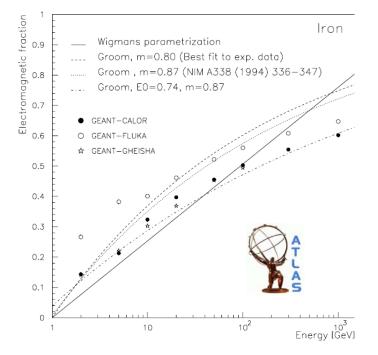
$$\frac{e}{\pi} = \frac{1}{f_{\rm em}(E_0) + (1 - f_{\rm em}(E_0)) \cdot h/e}$$

Popular parametrization by Groom et al.:

$$f_{\rm em}(E_0) = 1 - \left(\frac{E_0}{E_{\rm base}}\right)^{m-1}$$

m = 0.80 - 0.85, $E_{\rm base} = \begin{cases} 1.0 \text{ GeV} & \text{for } \pi^{\pm} \\ 2.6 \text{ GeV} & \text{for } p \end{cases}$

D.Groom et al., NIM A338, 336-347 (1994)





Hadronic Response (2)



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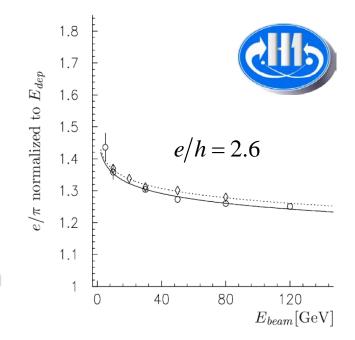
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$$\frac{e}{\pi} = \frac{e}{(E_0/E_{\text{base}})^{m-1}h + (1 - (E_0/E_{\text{base}})^{m-1})e}$$
$$= \frac{1}{1 - (1 - h/e)(E_0/E_{\text{base}})^{m-1}}$$

provides experimental access to characteristic calorimeter variables in pion test beams by fitting h/e, E_{base} and m from the energy dependence of the pion signal on electromagnetic energy scale:

$$\frac{e}{\pi} = \frac{E_0}{E_{\rm rec}^{\rm em}(\pi)} \approx \frac{E_{\rm dep}}{E_{\rm rec}^{\rm em}(\pi)}$$

Note that *e/h* is often constant, for example: in both H1 and ATLAS about 50% of the energy in the hadronic branch generates a signal independent of the energy itself



Complex mixture of hadrons and photons

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Not a single particle response Carries initial electromagnetic energy

Mainly photons

Very simple response model Assume the hadronic jet content is represented by 1 particle only Not realistic, but helpful to understand basic response features

More evolved model

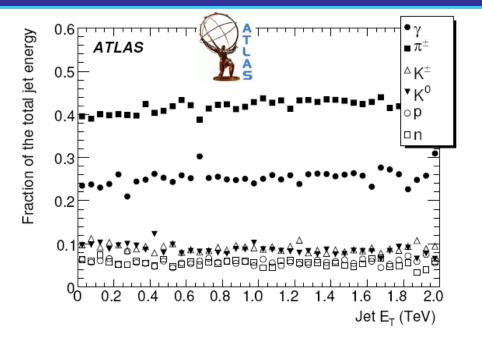
Use fragmentation function in jet response

This has some practical considerations

E.g. jet calibration in CDF

Gets non-compensation effect Does not address acceptance

effect due to shower overlaps





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$$\frac{j(E_{jet})}{e} = f_{\gamma}^{jet} + \left(1 - f_{\gamma}^{jet}\right) \cdot \left(f_{em} + \left(1 - f_{em}\right)\frac{h}{e}\right)$$

$$f_{
m em}=f_{
m em}$$
 (${m E}_{
m jet}^{
m had}$), ${m E}_{
m jet}^{
m had}=\!\left({f 1}\!-\!f_{\gamma}^{
m jet}
ight)\!{m E}_{
m jet}$

[single particle approximation]

$$f_{\rm em} = 1 - \left(\frac{E_{\rm jet}^{\rm had}}{E_{\rm base}}\right)^{1-m}$$

[Groom's parameterization]

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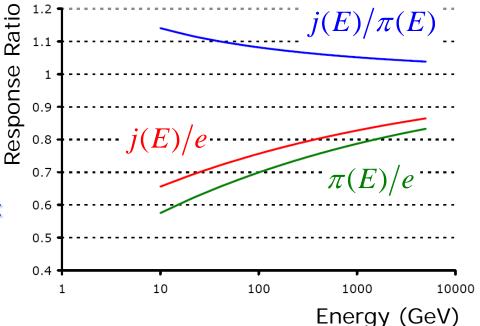
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 $= f_{\nu}^{\text{jet}}$

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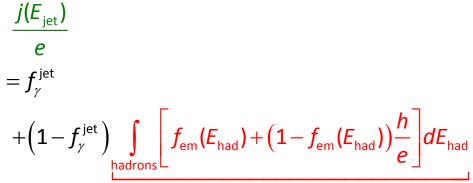
Use fragmentation function in jet $= f_{\gamma}^{\text{jet}} + (1 - f_{\gamma}^{\text{jet}}) \sum (1 + (E_{\text{had}}/E_{\text{base}})^{m-1} (h/e-1))$ response

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composition of hadronic component given by jet fragmentation function

$$+ \left(1 - f_{\gamma}^{\text{jet}}\right) \sum_{\text{hadrons}} \left[1 - \left(\frac{E_{\text{had}}}{E_{\text{base}}}\right)^{m-1} + \left(\frac{E_{\text{had}}}{E_{\text{base}}}\right)^{m-1} h/e\right]$$

$$\sum (1+(E))$$



Fluctuations of the "zero" or "empty" signal reading

Pedestal fluctuations

Independent of the signal from particles

At least to first order

Mostly incoherent

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No noise correlations between readout channels

Noise in each channel is independent oscillator

Gaussian in nature

Pedestal fluctuations ideally follow normal distribution around 0 Width of distribution (1 σ) is noise value

Signal significance

Noise can fake particle signals

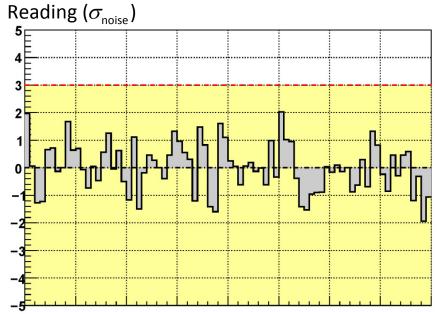
Only signals exceeding noise can be reliably measured

Signals larger than 3 × noise are very likely from particles

Gaussian interpretation of pedestal fluctuations

Calorimeter signal reconstruction aims to suppress noise

Average contribution = 0, but adds to fluctuations!



Spatial Coordinate/Calorimeter Cell

Small signal:

Noise only

Signal on top of noise Sum of noise and signal Signal after noise suppression



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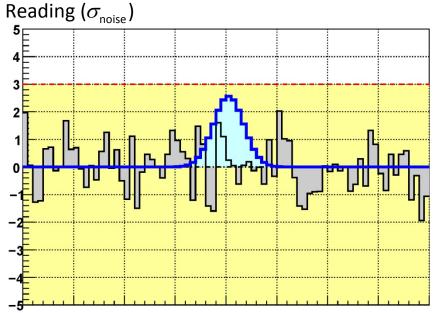
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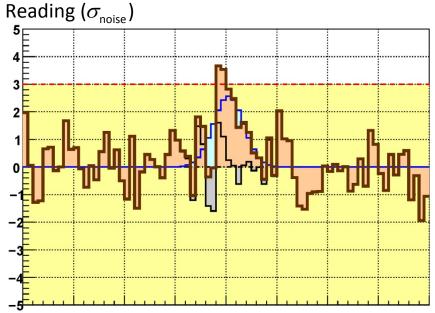
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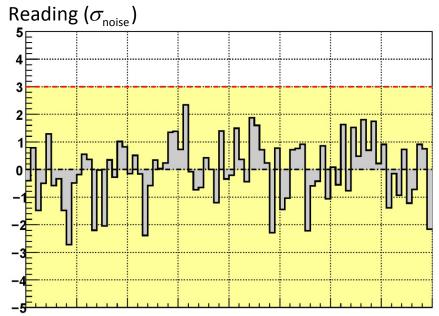
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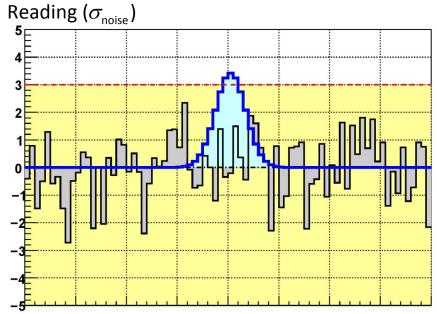
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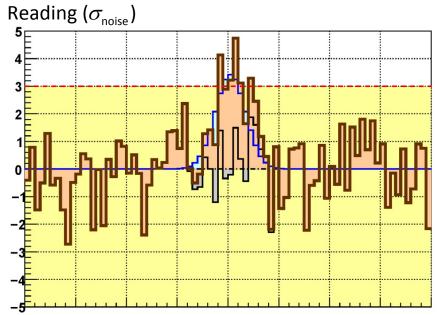
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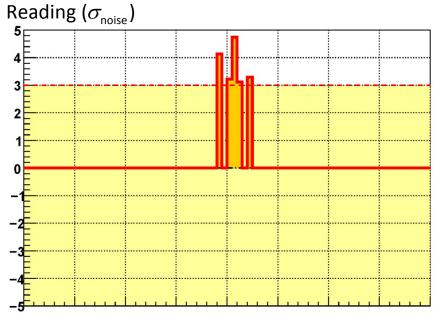
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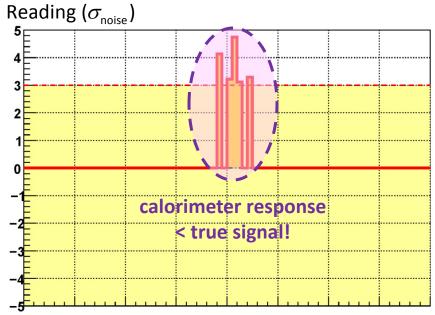
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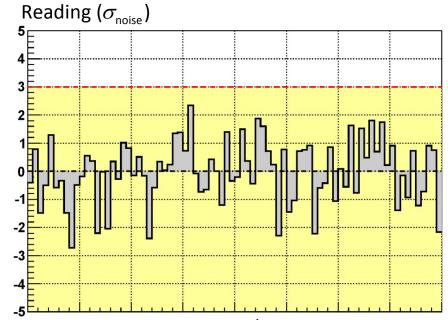
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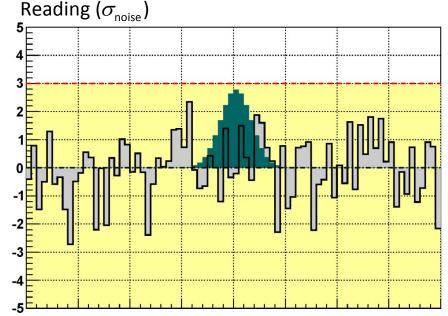
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Noise only Signal on top of noise



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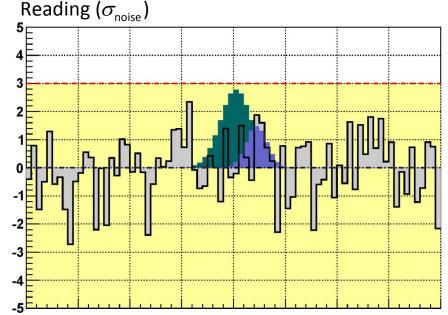
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Small signal, first and second particle:

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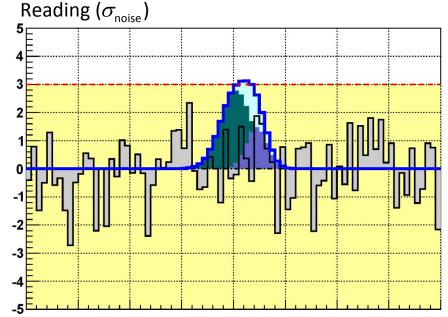
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Small signal, two particle, sum:

Noise only Signal on top of noise



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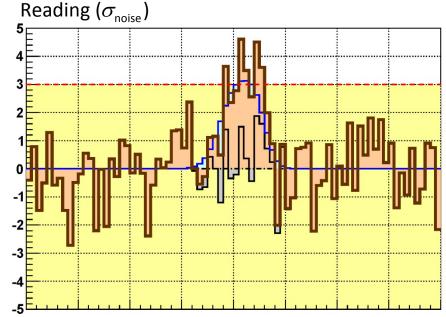
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Noise only Signal on top of noise

Sum of noise and signal



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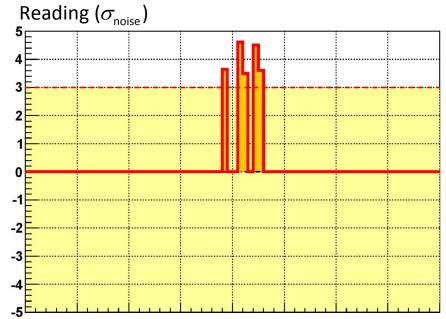
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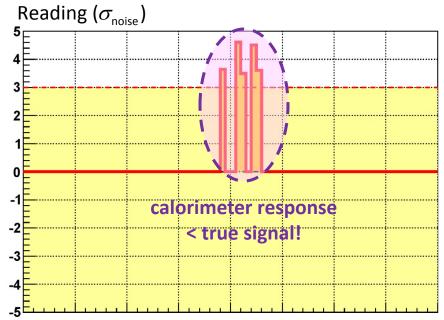
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Small signal, two particles:

Noise only

- Signal on top of noise
- Sum of noise and signal
- Signal after noise suppression