



Classes

B&N: “Scientific and engineering problems are rarely posed directly in terms of the computer’s intrinsic types: bits, bytes, integers and floating point numbers”

Shocking statement?

In a detector’s tracking code, for example, the problem is posed in terms of...

- tracks
- points
- list of points
- chamber
- cylinders
- layers

C++ with its mechanism of *classes* allows defining new types and the operations on these types

When we do object-oriented programming with C++ we will be writing and using classes



Examples from CLHEP

Class Library for High Energy Physics

Why?

- Provide some classes are specific to HEP
- Encourage code sharing between experiments and between experimentalists and theorists.
- Reduce redundant work

Who?

- started by Leif Lönnblad, Nordita (via CERN, DESY and Lund)
- now maintained by committee

Use

- `http://proj-clhep.web.cern.ch/proj-clhep/`
- will show version 1.4
- current is 2.0



ThreeVector

CLHEP's ThreeVector class (simplified)

```
class Hep3Vector {
public:
    Hep3Vector();
    Hep3Vector(double x, double y, double z);
    Hep3Vector(const Hep3Vector &v);
    double x();
    double y();
    double z();
    double phi();
    double cosTheta();
    double mag();
    // much more not shown
private:
    double dx, dy, dz;
};
```

- this is the declaration in the header file
- keyword `class` starts the declaration which is contained within the `{ }`
- class contains member functions
- an object can be an instance of a class
- an object of a class contains data members



Using a class object

Consider

```
#include <iostream>
#include <CLHEP/ThreeVector.h>
using namespace std;

int main() {
    double x, y, z;

    while ( cin >> x >> y >> z ) {
        Hep3Vector aVec(x, y, z);

        cout << "r: " << aVec.mag();
        cout << " phi: " << aVec.phi();
        cout << " cos(theta): " << aVec.cosTheta() << endl;
    }
    return 0;
}
```

- `Hep3Vector aVec(x, y, z);` declares `aVec`, a object of type `Hep3Vector` and initializes it
- `aVec.mag()` calls the member function `mag()` of the object
- the “.” is the *class member access operator*
- use “->” access operator when one has pointer to object:



Data members

Look again

```
class Hep3Vector {
public:
    // member functions

private:
    double dx, dy, dz;
};
```

- `Hep3Vector` contains 3 data members
- declaration is like any other except no initializers are allowed
- every instance of the class `Hep3Vector` will have its own 3 data members.

```
Hep3Vector x(1.0, 0.0, 0.0);
Hep3Vector y(0.0, 1.0, 0.0);
Hep3Vector z(0.0, 0.0, 1.0);
```

- `Hep3Vector` is a type
- an object of type `Hep3Vector` has a value (or state) that is represented by the values of its data members (like a complex number)
- the size of a `Hep3Vector` object is likely to be `3*sizeof(double)`

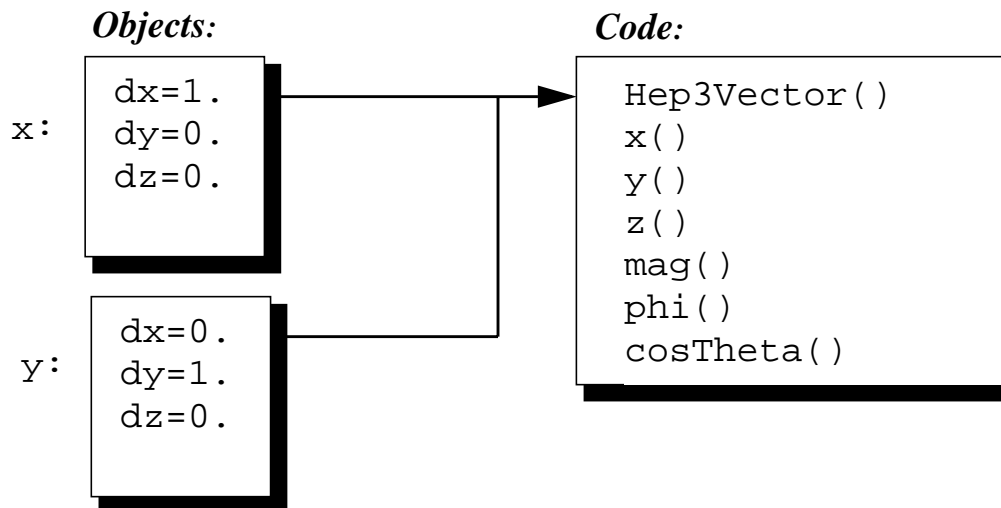


Memory model

Consider

```
Hep3Vector x(1.0, 0.0, 0.0);  
Hep3Vector y(0.0, 1.0, 0.0);
```

In computer's memory we have



- an object is an instance of a class (type)
- each object has its own data members
- one copy of the code for a class is shared by all instances of the class
- hidden argument `this` is how it all works



Use of `private` keyword

We have

```
class Hep3Vector {
public:
    double mag();
    double x();
    double dummy;
    // member functions

private:
    double dx, dy, dz;
};
```

- the following compiles

```
Hep3Vector x(1.0, 0.0, 0.0);
cout << x.dummy;
```

- the following does not compile

```
Hep3Vector x(1.0, 0.0, 0.0);
cout << x.dx; // WRONG
```

- this is called *data hiding*
- by disallowing direct access, you hide how data is stored.
- one can change how data is stored without breaking user code because you disallowed direct access



Initializing a class object

At least 3 ways we would like to initialize an object

- no initial value

```
Hep3Vector a;
```

- with three double values

```
Hep3Vector a(1.0, 1.0, 1.0);
```

- copy of another object

```
Hep3Vector a(1.0, 1.0, 0.0);  
Hep3Vector b = a;
```

- each calls a special member function called a *constructor*

There are three constructors in the class

```
class Hep3Vector {  
public:  
    Hep3Vector();  
    Hep3Vector(double x, double y, double z);  
    Hep3Vector(const Hep3Vector &v);  
    // much more not shown  
private:  
    double dx, dy, dz;  
};
```




Constructor Implementations

The constructor member functions

```
Hep3Vector::Hep3Vector(double x, double y, double z) {  
    dx = x;  
    dy = y;  
    dz = z;  
}  
  
Hep3Vector::Hep3Vector(const Hep3Vector &vec) {  
    dx = vec.dx;  
    dy = vec.dy;  
    dz = vec.dz;  
}  
  
Hep3Vector::Hep3Vector() {  
}
```

- called after memory space has been allocated
- when the class name and member name are the same, then the member function is a constructor
- `Foo::bar()` says that `bar()` is a member function of the class `Foo`
- `::` is the *scope resolution operator*
- note that copy constructor uses a const reference



Data Hiding

Violation of private parts?

```
Hep3Vector::Hep3Vector(const Hep3Vector &vec) {  
    dx = vec.dx;  
    dy = vec.dy;  
    dz = vec.dz;  
}
```

- objects of the same class have access to private data members
- the purpose of data hiding is to hide implementation from other classes
- can't hide implementation from object of same class
- `const` qualifier says we wouldn't change argument



Access member functions

The declaration was

```
class Hep3Vector {
public:
    double x();
    double y();
    double z();
    // much more not shown
private:
    double dx, dy, dz;
};
```

The implementation is

```
double Hep3Vector::x() {
    return dx;
}
double Hep3Vector::y() {
    return dy;
}
double Hep3Vector::z() {
    return dz;
}
```

- inefficient?
- make function in-line
- always ask: “do I want the data to do some work or do I want the object to do the work”



Inline access member functions

Change declaration to

```
inline double Hep3Vector::x() {  
    return dx;  
}  
inline double Hep3Vector::y() {  
    return dy;  
}  
inline double Hep3Vector::z() {  
    return dz;  
}
```

- can be used when execution of function body is shorter than time to call and return from function
- any decent compiler should produce inline code instead of function call for above
- inline keyword is just a hint, however
- data hiding is preserved
- implementation needs to be in the header file
- sometimes put in file with `.icc` suffix that is included by the header file (not BaBar practice)
- program could be faster
- program could be larger



More Implementation

Recall

```
class Hep3Vector {
public:
    double mag();
    double phi();
    double cosTheta();
    // much more not shown
private:
    double dx, dy, dz;
};
```

Implementation

```
inline double Hep3Vector::mag() {
    return sqrt(dx*dx + dy*dy + dz*dz);
}

inline double Hep3Vector::phi() {
    return dx == 0.0 && dy == 0.0 ? 0.0 : atan2(dy,dx);
}

inline double Hep3Vector::cosTheta() {
    double ptot = mag();
    return ptot == 0.0 ? 1.0 : dz/ptot;
}
```

- note how object calls its own member function
- examples of letting object do the work



Design decisions

Fortran style

```
common/points/hits(3,100)
real*4      hits
real*4 x, y, z, r
! do some work
x = hits(1,i) ! or from ZEBRA bank
y = hits(2,i)
z = hits(3,i)
r = sqrt(x*x + y*y + z*z);
```

Another Fortran style

```
common/points/hits(3,100)
real*4      hits
real*4 x, y, z, r
! do some work
x = hits(1,i)
y = hits(2,i)
z = hits(3,i)
r = mag(x, y, z) ! or mag(hits(1,i))
```

Mark II VECSUB style

```
common/points/hits(3,100)
real*4 r
! do some work
r = hitsmag(i)
```



C++ design

C++ style

```
Hep3Vector hits[100];  
// do some work  
double r = hits[i].mag();
```

- efficient with inline functions
- don't need knowledge of data structure
- modular
- re-usable
- later, we'll get rid of the fixed or dynamic arrays



Homework

Suppose

```
class Hep3Vector {
public:
    Hep3Vector();
    Hep3Vector(double x, double y, double z);
    Hep3Vector(const Hep3Vector &v);
    inline double x();
    inline double y();
    inline double z();
    inline double phi();
    inline double cosTheta();
    inline double mag();
private:
    double r, cos_theta, phi;
};
```

- write the implementation for this class
- constructors take x, y, and z as arguments, but must initialize r, cos(theta), and phi data members
- try test program shown before, it should still work with this small change

```
// #include <CLHEP/ThreeVector.h>
#include "ThreeVector.h"
```

- write a program to exercise `x()`, `y()`, and `z()` member functions



Another look at Hep3Vector

We'll now look at the real `Hep3Vector` class and explain those new language elements we need to understand it

```
class Hep3Vector {
public:
    Hep3Vector(double x=0., double y=0., double z=0.);
    Hep3Vector(const Hep3Vector&);
    double x() const;
    double y() const;
    double z() const;
    double phi() const;
    double cosTheta() const;
    double mag() const;
    // much more not shown
private:
    double dx, dy, dz;
};
```

- uses default arguments
- `const` keyword after function means no data member of the object will be changed by invoking function
- this `const` is enforced when compiling the class
- the above are obvious, but it will be less obvious with other classes in the future



Initializing syntax

Two forms to invoke copy constructor

```
Hep3Vector x(1.0, 0.0, 0.0);  
Hep3Vector y = x; // C style  
Hep3Vector y(x); // C++ class style
```

- the two are equivalent if argument is same type as object being declared
- both invoke copy constructor
- the = form allows user defined conversions when argument is not same type
- both forms allowed for built-in type

Consider

```
Hep3Vector x = 1.0;
```

- might be equivalent to

```
Hep3Vector tmp(1.0);  
Hep3Vector x = tmp;
```

- but following has no surprises

```
Hep3Vector x(1.0);
```



Member Initializers

The constructor can be implemented like any other member function...

```
Hep3Vector::Hep3Vector(double x, double y, double z){  
    dx = x;  
    dy = y;  
    dz = z;  
}
```

- but data members need to be constructed before assignment
- for `Hep3Vector` the custom constructor would be called

An alternate form is use of member initializers

```
Hep3Vector::Hep3Vector(double x, double y, double z) :  
    dx(x), dy(y), dz(z) {}
```

- note the `:` preceding the opening `{`
- `dx(x)` notation calls a constructor directly
- which constructor depends on argument matching
- in the above case, it is the copy constructor
- the function body is required, even if empty



Function Return Types

A function returns a temporary hidden variable that is initialized by the return statement

Consider

```
float f() {  
    return 1;  
}  
float x;  
// ...  
x = f();
```

- it is as if

```
float tmp = 1;  
x = tmp;
```

Consider

```
float & Vector3::x() {  
    return dx;  
}  
Vector3 vec;  
// ...  
vec.x() = 1.0; // uh?
```

- it is as if

```
float &tmp = vec.dx;  
tmp = 1.0;
```



Operators are functions?

Operators can be thought of as functions

```
double add( double a, double b) {
    return a + b;
}
double x, y, z;
//
z = x + y;
z = add(x, y);
```

- `add()` operates on two arguments and returns a result
- the symbol `+` operates on two operands and returns a result

Use of mathematical symbols is more concise and easier to read

```
double add( double a, double b);
double mul( double a, double b);
double a, b, x, y, z;
//
z = add(mul(a, x), mul(b, y));
z = a*x + b*y;
```

C, C++, and Fortran all define operators for built-in types



Operator Functions

An operator function in `Hep3Vector`

```
class Hep3Vector {  
public:  
    inline Hep3Vector& operator +=(const Hep3Vector &);  
    // more not shown
```

- the name of the function is the word `operator` followed by the operator symbol
- this function is called when

```
Hep3Vector p, q;  
//  
q += p;
```

- the function is invoked on `q`; the left-hand side
- the argument will be `p`; the right-hand side
- `q += p;` is shorthand for `q.operator+=(p);`
- the function returns a `Hep3Vector` reference for consistency with built-in types

```
Hep3Vector p, q, r;  
//  
r = q += p;  
// r.operator=( q.operator+=(p) )
```



Operator Function Implementation

Implementation

```
inline Hep3Vector& Hep3Vector::operator+=(const Hep3Vector& p) {  
    dx += p.x(); // could have been dx += p.dx  
    dy += p.y();  
    dz += p.z();  
    return *this;  
}
```

- does the accumulation as one would expect
- `this` is a hidden argument that is a pointer to the object's own self
- `this->dx` is thus equivalent to `dx`
- remember: use `->` instead of `.` when you have a pointer
- or `dx` is shorthand for `this->dx`
- recall that `Hep3Vector::x()` is an in-line function itself
- `return *this` returns the address of the object, thus the reference



Compare Fortran and C++

Fortran vector sum

```
real p(3), q(3)
! ...
q(1) = q(1) + p(1)
q(2) = q(2) + p(2)
q(3) = q(3) + p(3)
```

C++ vector sum

```
Hep3Vector p, q;
// ...
q += p;
```




Operator Functions

Essentially all operators can be used for user defined types except `."`, `.*`, `::`, `sizeof` and `?:`

Can not define new ones

- sorry, can't do `operator**()` for exponentiation
- and there's no operator one could use with the correct precedence
- can't overload operators for built-in types

One should only use when conventional meaning makes sense

```
Hep3Vector p, q;  
double z;  
// .....  
z = p*q; // uh?
```

- is this cross product or dot product?
- `Hep3Vector` defines it to be dot product



Non-member Operator Function

Consider

```
inline Hep3Vector operator*(const Hep3Vector& p, double a) {  
    Hep3Vector q( a*p.x(), a*p.y(), a*p.z() );  
    return q;  
}
```

- invoked by

```
double scale = 3.0;  
Hep3Vector p(1.0); // unit vector along x axis  
Hep3Vector r(0.0, 1,0);  
r += p*scale;
```

- note return by value
- need a new object whose value is $x*scale$
- the temporary object is used as argument to `operator+=()` and then discarded
- such temporary objects are generated by Fortran as well

```
real scale, p(3), r(3)  
r(1) = r(1) + p(1)*scale  
r(2) = r(2) + p(2)*scale  
r(3) = r(3) + p(3)*scale
```



Need Symmetric Operator Functions

CLHEP has

```
inline Hep3Vector operator*(const Hep3Vector& p, double a) {  
    Hep3Vector q( a*p.x(), a*p.y(), a*p.z() );  
    return q;  
}  
inline Hep3Vector operator*(double a, const Hep3Vector& p) {  
    Hep3Vector q( a*p.x(), a*p.y(), a*p.z() );  
    return q;  
}
```

- second one invoked by

```
double scale = 3.0;  
Hep3Vector p(1.0); // unit vector along x axis  
Hep3Vector q(0.0, 1,0);  
q += scale*p;
```

- argument matching applies
- must use global function because `scale.operator*(p)` doesn't exist



The Complete List - I

Constructors

```
Hep3Vector(double x=0.0, double y=0.0, double z=0.0);  
Hep3Vector(const Hep3Vector &);
```

- also contains conversion constructor

Destructor

```
~Hep3Vector();
```

- invoked when object is deleted (more next session)

Accessor-like functions

```
inline double x() const;  
inline double y() const;  
inline double z() const;  
inline double mag() const;  
inline double mag2() const;  
inline double perp() const;  
inline double perp2() const;  
inline double phi() const;  
inline double cosTheta() const;  
inline double theta() const;  
inline double angle(const Hep3Vector &) const;  
inline double perp(const Hep3Vector &) const;  
inline double perp2(const Hep3Vector &) const;
```



The Complete List - II

Manipulators

```
void rotateX(double);  
void rotateY(double);  
void rotateZ(double);  
void rotate(double angle, const Hep3Vector & axis);  
Hep3Vector & operator *= (const HepRotation &);  
Hep3Vector & transform(const HepRotation &);
```

Set functions

```
inline void setX(double);  
inline void setY(double);  
inline void setZ(double);  
inline void setMag(double);  
inline void setTheta(double);  
inline void setPhi(double);
```

Output function

```
ostream & operator << (ostream &, const Hep3Vector &);
```

- allows

```
Hep3Vector x(1.0);  
// ...  
cout << x << endl;
```



The Complete List - III

Vector algebra member functions

```
inline double dot(const Hep3Vector &) const;  
inline Hep3Vector cross(const Hep3Vector &) const;  
inline Hep3Vector unit() const;  
inline Hep3Vector operator - () const;
```

Vector algebra non-member functions

```
Hep3Vector operator+(const Hep3Vector&, const Hep3Vector&);  
Hep3Vector operator-(const Hep3Vector&, const Hep3Vector&);  
double operator * (const Hep3Vector &, const Hep3Vector &);  
Hep3Vector operator * (const Hep3Vector &, double a);  
Hep3Vector operator * (double a, const Hep3Vector &);
```

Assignment operators

```
inline Hep3Vector & operator = (const Hep3Vector &);  
inline Hep3Vector & operator += (const Hep3Vector &);  
inline Hep3Vector & operator -= (const Hep3Vector &);  
inline Hep3Vector & operator *= (double);
```



Summary

Hep3Vector implements vector algebra

It was long and tedious to implement

**Now that we have it (thank you, Leif and Anders),
we can use it and never have to expand these details
in our own code**

**Besides objects of type `int`, `float`, and `double`,
we can use operators with objects of type
`Hep3Vector`**

We have a new type with higher level of abstraction



Levels of Abstraction in Physics

Do you recognize these equations?

$$\sum_i \frac{\partial E_i}{\partial x_i} = \frac{\partial E_x}{\partial x} + \frac{\partial E_y}{\partial y} + \frac{\partial E_z}{\partial z} = 4\pi\rho$$

$$\sum_i \frac{\partial B_i}{\partial x_i} = \frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} + \frac{\partial B_z}{\partial z} = 0$$

$$\sum_i \varepsilon_{ijk} \frac{\partial}{\partial x_j} E^k = -\frac{1}{c} \frac{\partial B_i}{\partial t}$$

$$\frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z} = -\frac{1}{c} \frac{\partial B_x}{\partial t}$$

$$\frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x} = -\frac{1}{c} \frac{\partial B_y}{\partial t}$$

$$\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} = -\frac{1}{c} \frac{\partial B_z}{\partial t}$$



Higher Level of Abstraction

Now do you recognize them?

$$\vec{\nabla} \cdot \mathbf{E} = 4\pi\rho$$

$$\vec{\nabla} \times \mathbf{B} = \frac{4\pi}{c} \mathbf{J} + \frac{1}{c} \frac{\partial \mathbf{E}}{\partial t}$$

$$\vec{\nabla} \cdot \mathbf{B} = 0$$

$$\vec{\nabla} \times \mathbf{E} = -\frac{1}{c} \frac{\partial \mathbf{B}}{\partial t}$$

or even

$$\partial_\alpha F^{\alpha\beta} = \frac{4\pi}{c} J^\beta$$

$$\frac{1}{2} \epsilon^{\alpha\beta\gamma\delta} \partial_\alpha F_{\gamma\delta} = 0 = \partial^\alpha F^{\beta\gamma} + \partial^\beta F^{\gamma\alpha} + \partial^\gamma F^{\alpha\beta}$$

To advance in physics/math, we need higher levels of abstractions, else we get lost in implementation details

C++ allows higher level of abstract as well